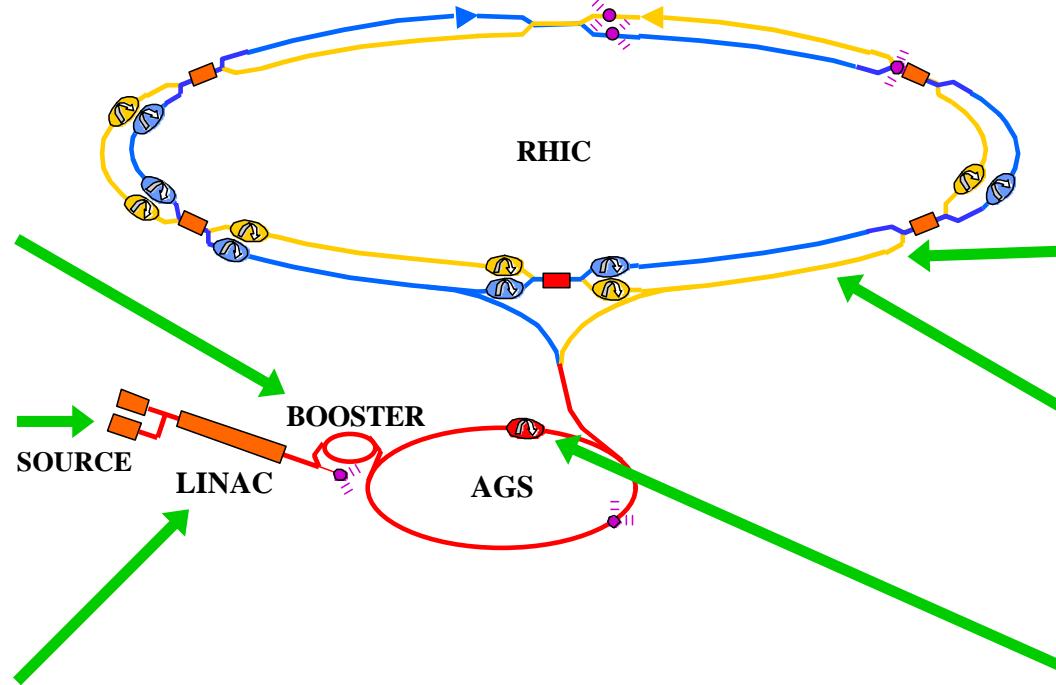
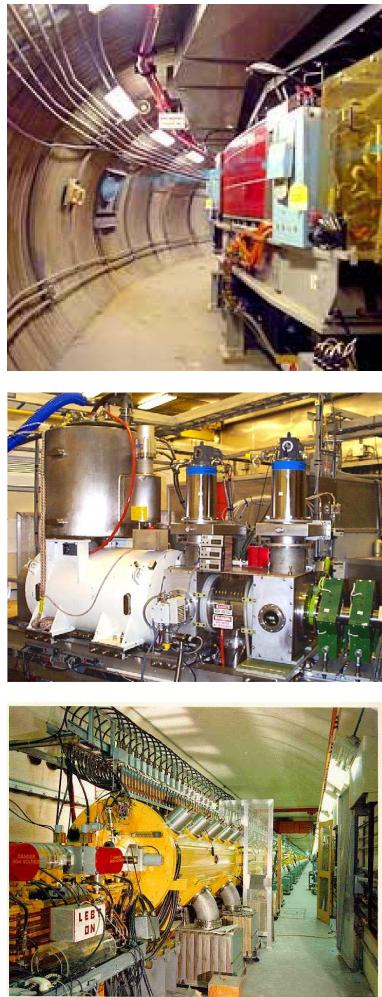


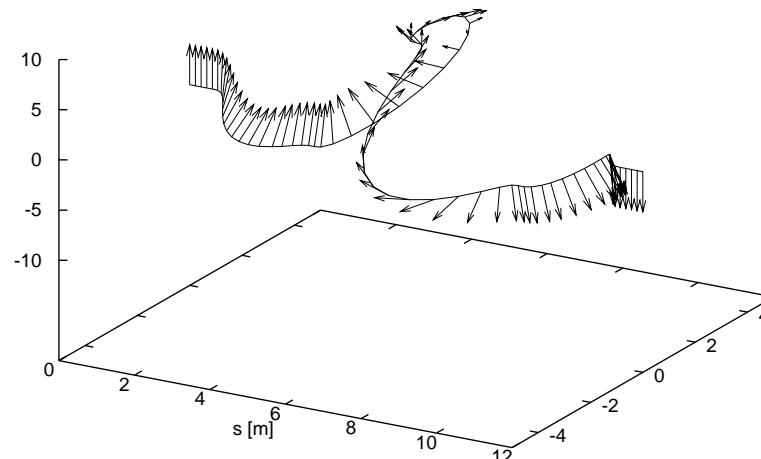
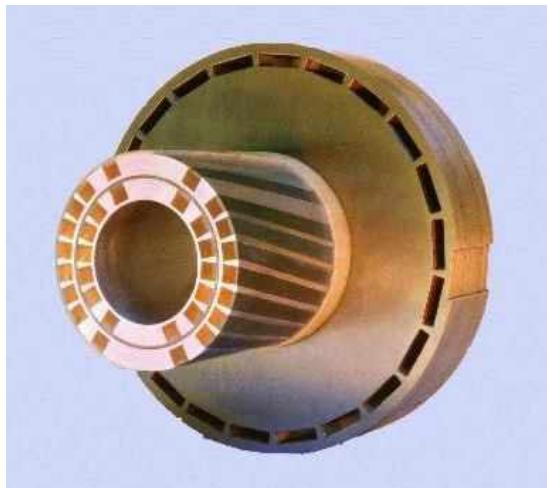
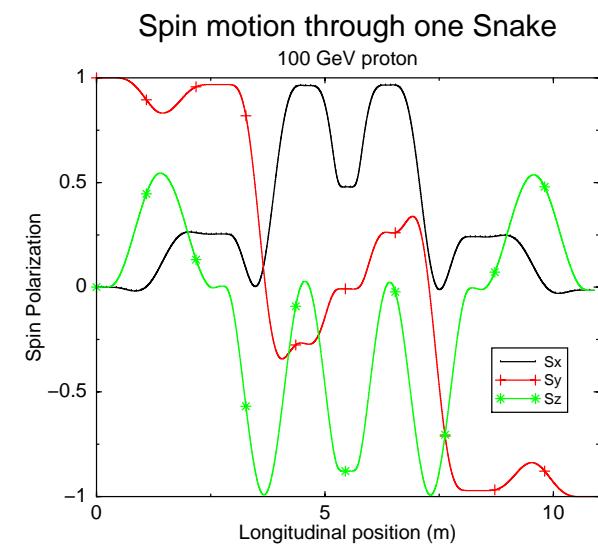
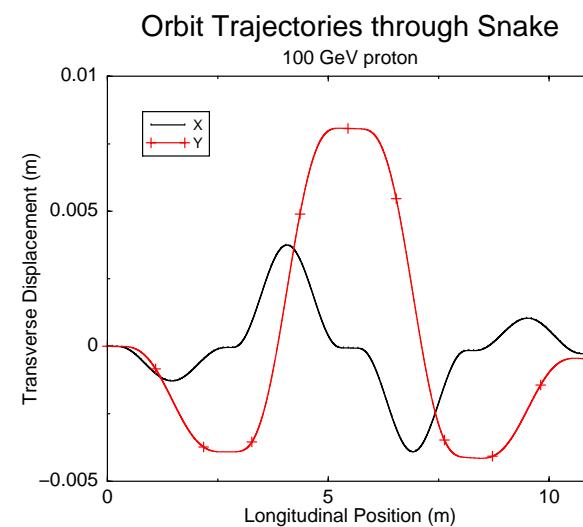
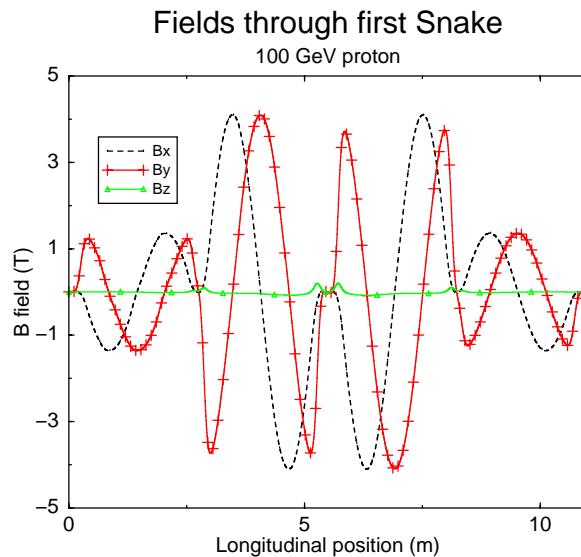
Accelerator Complex (Pol. Protons)

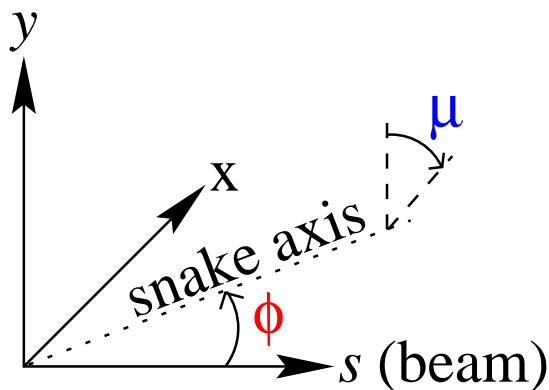


LINAC: Linear Accelerator
AGS: Alternating Gradient Synchrotron
RHIC: Relativistic Heavy Ion Collider



_trajectory and Spin through Snakes

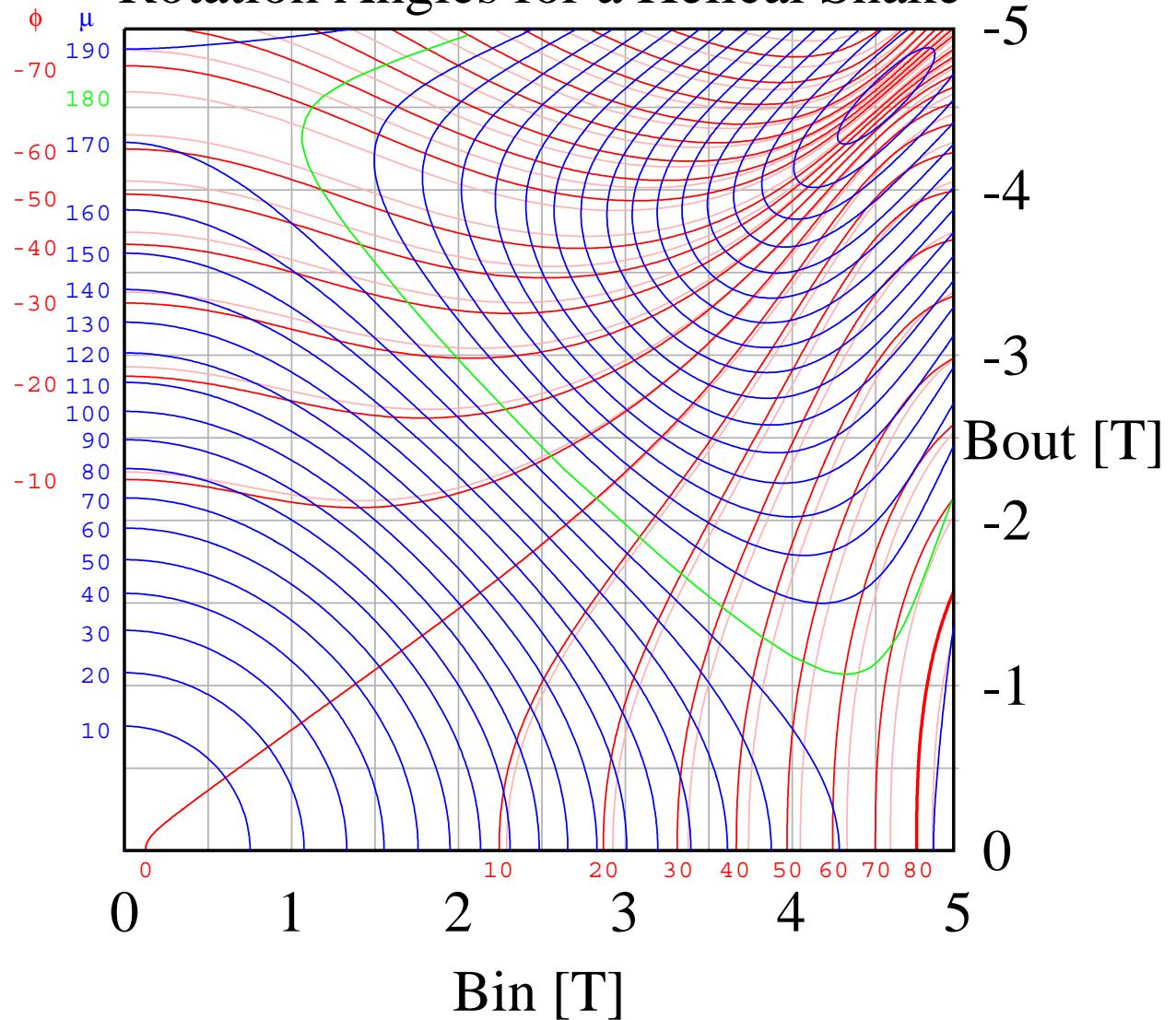




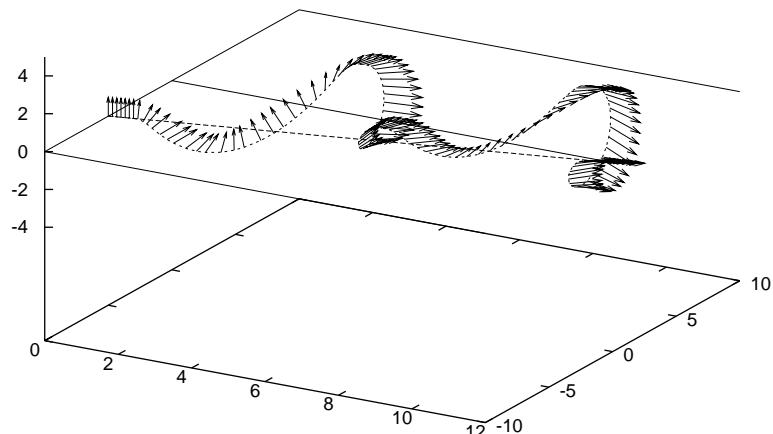
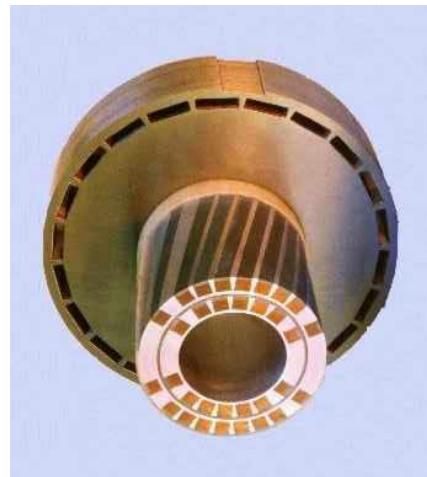
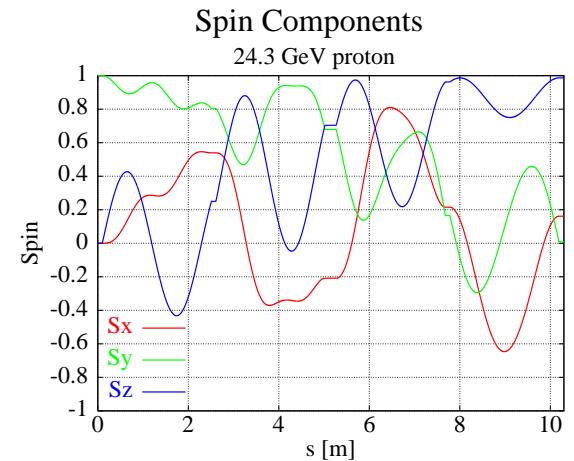
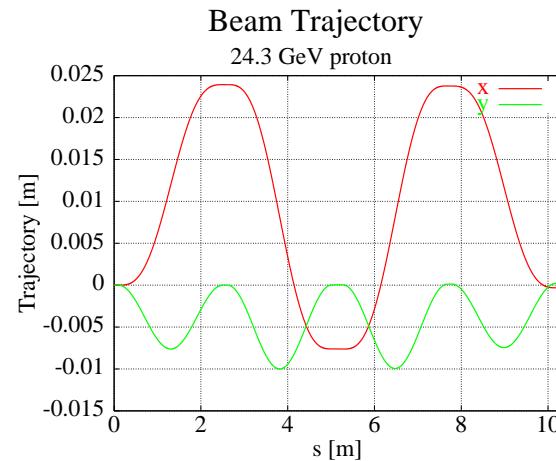
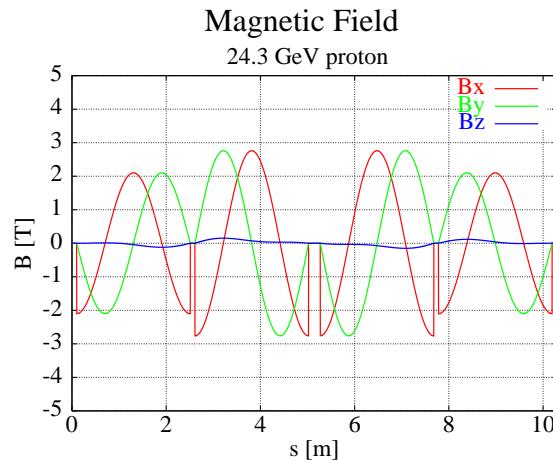
The rotation axis of the snake is ϕ , and μ is the rotation angle.

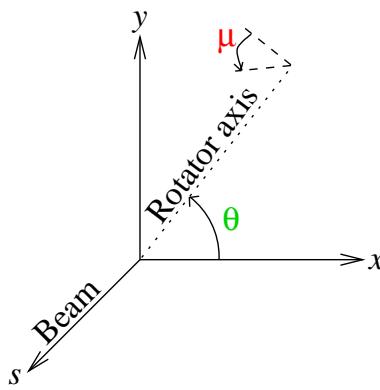
Note that the ϕ contours shift slightly from injection (red) at 25 GeV to storage (pink) at 250 GeV.

Rotation Angles for a Helical Snake



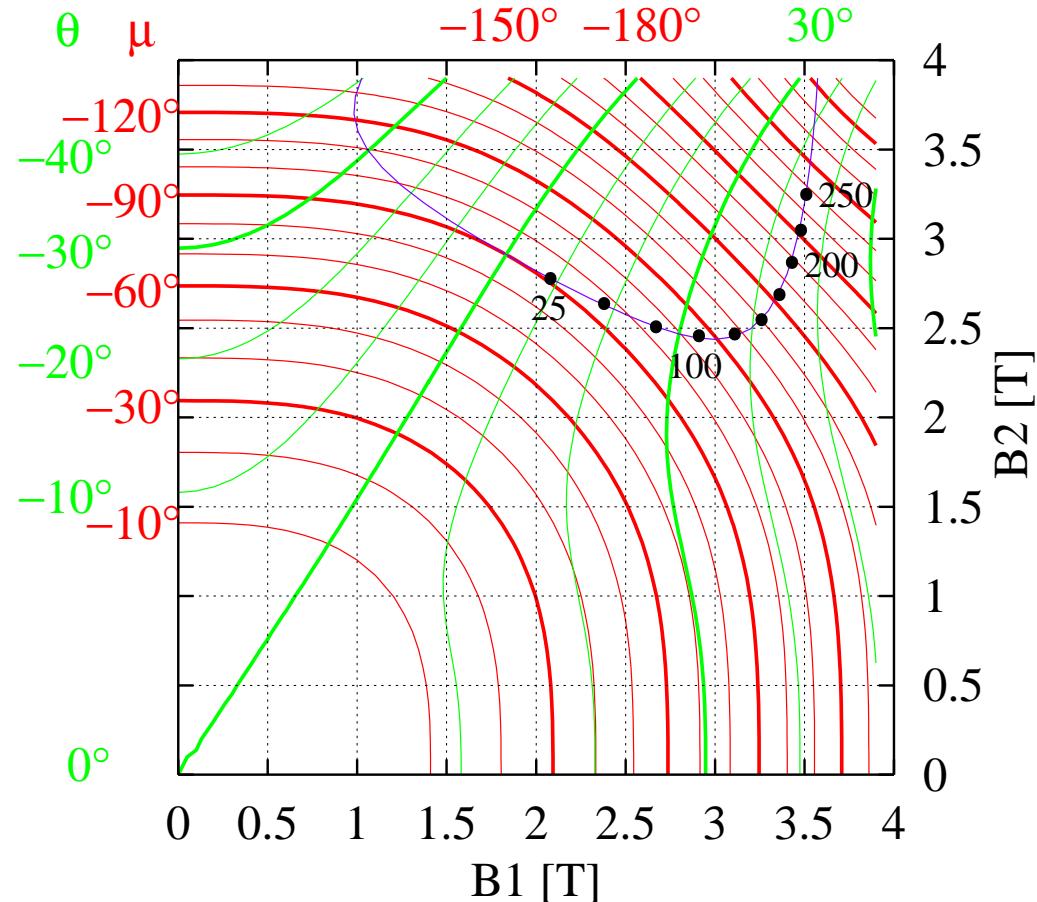
Helical Spin Rotators





The rotation axis of the spin rotator is in the x - y plane at an angle θ from the vertical. The spin is rotated by the angle μ around the rotation axis.

Rotation Angles for a Helical Spin Rotator



Note: Purple contour for rotation into horizontal plane.
Black dots show settings for RHIC energies in increments of 25 GeV from 25 to 250 GeV.

§ Rotator Axes and Precession §

To precess the spin from vertical into the horizontal plane:

$$\sin \beta = \sin \mu \cos \theta$$

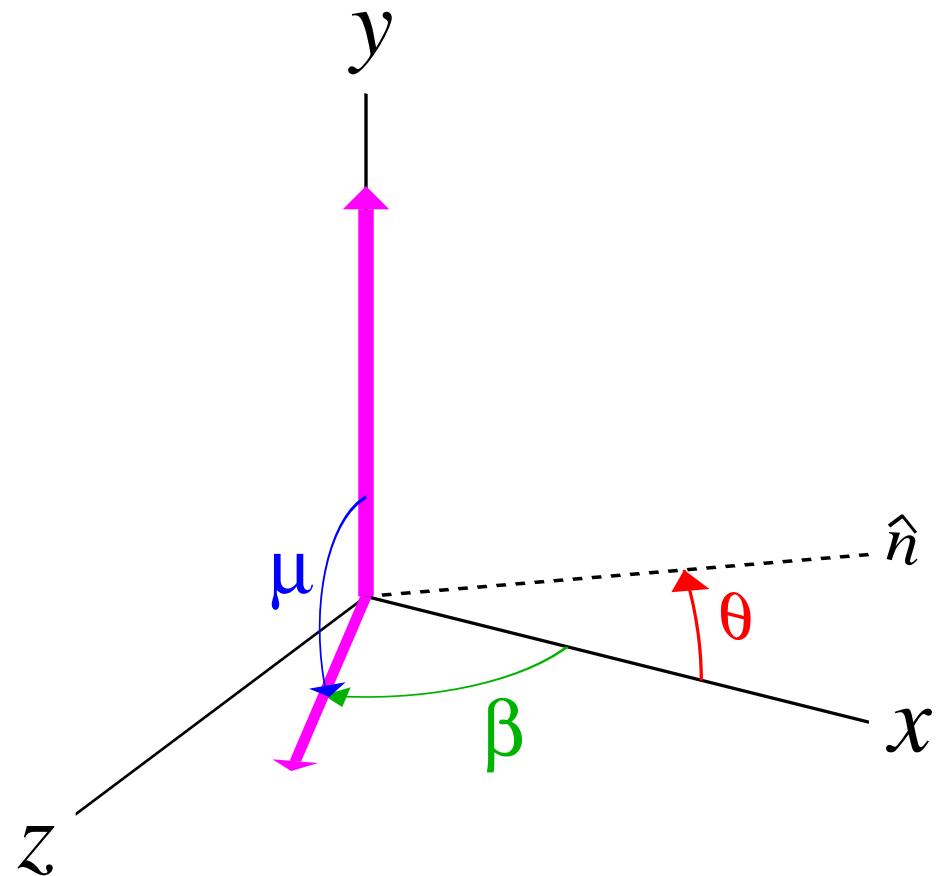
$$\cos \mu = -\tan^2 \theta$$

$$\mu \in [90^\circ, 270^\circ]$$

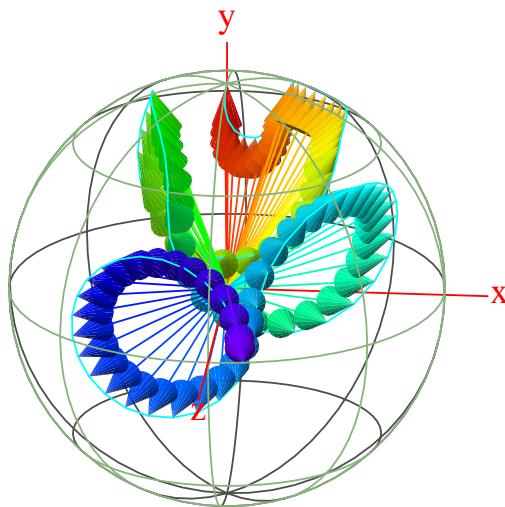
$$\theta \in [-45^\circ, 45^\circ] \cup [135^\circ, 225^\circ]$$

For longitudinal polarization want:

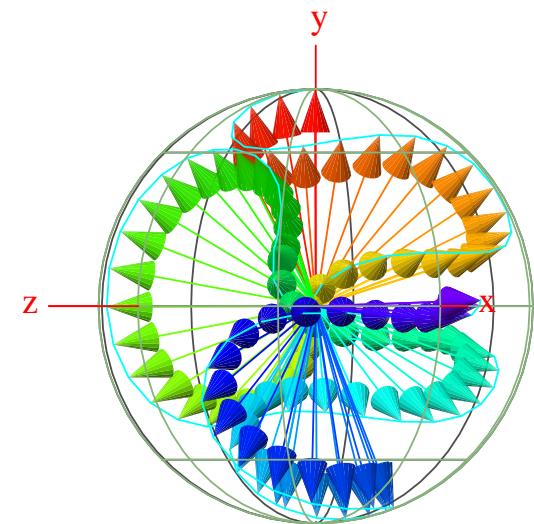
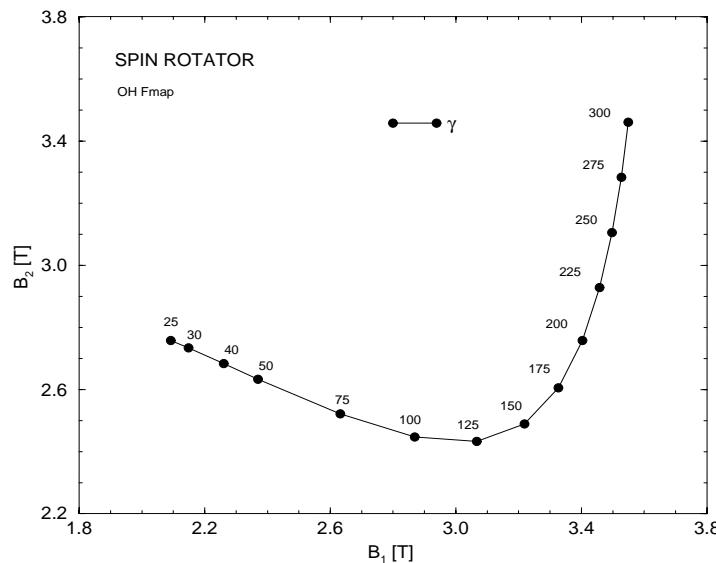
$$\beta = G\gamma \times \theta_{D0DX}$$



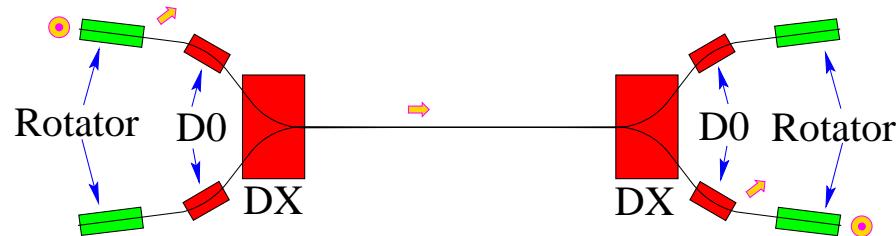
Compensation for D0-DX Bends



$E = 25 \text{ GeV}$
D0DX: 10° precession



$E = 250 \text{ GeV}$
D0DX: 100° precession



𝓁 Formulae for a Single Rotator Helix 🔍

Parameters for a single RHIC rotator helix

Pitch: $k = \frac{2\pi}{\lambda}$, $\lambda = 2.41$ m [$+(-)$ for right(left)-handed]

$$\kappa = \frac{q}{p}(1 + G\gamma)B$$

$$\text{Rotation axis: } \hat{n} = \frac{k\hat{z} + \kappa\hat{x}}{\sqrt{\kappa^2 + k^2}}$$

$$\text{Precession angle: } \alpha = 2\pi \left(\sqrt{1 + \left(\frac{\kappa}{k}\right)^2} - 1 \right)$$

$$\text{Transverse offset: } \Delta x = \frac{q}{p} \frac{B\ell}{k} = \frac{q}{p} \frac{\lambda^2}{2\pi} B$$

Scaling Snakes and Rotators to He³

Scaling of the field at maximum energy:

The maximum rigidity of the beams must be the same: $r_{\max} = \frac{p}{q} = 834$ Tm

$$\gamma_{\text{He}^3} \simeq \frac{Z}{A} \gamma_p$$

Want the same precession, so κ must be the same.

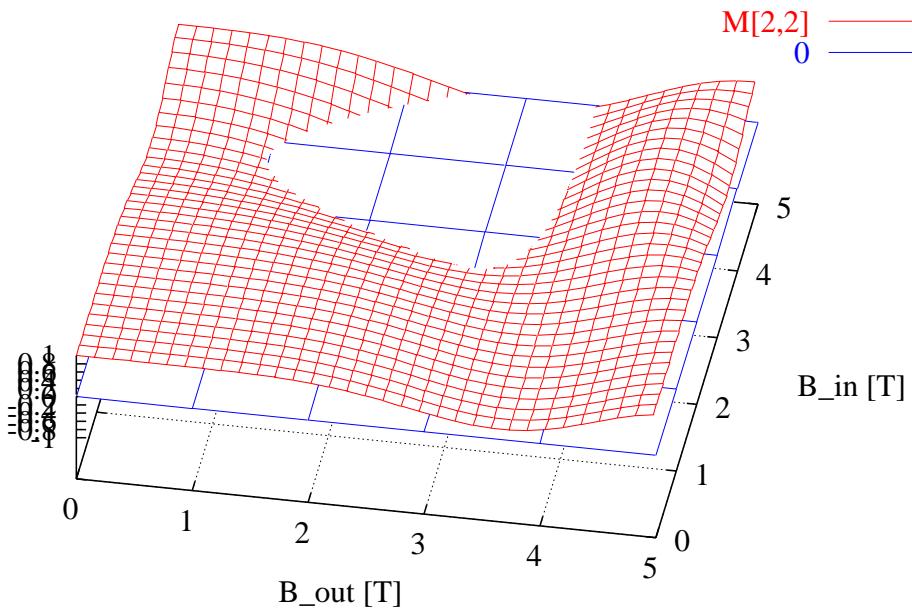
$$\begin{aligned} B_{\text{He}^3} &\simeq \frac{1 + G_p \gamma_p}{1 + G_{\text{He}^3} \gamma_{\text{He}^3}} B_p \\ &\simeq \frac{AG_p}{ZG_{\text{He}^3}} \simeq -0.643 \end{aligned}$$

Snake excursion at injection $r_{\text{inj}} = 81.1$ Tm (for protons):

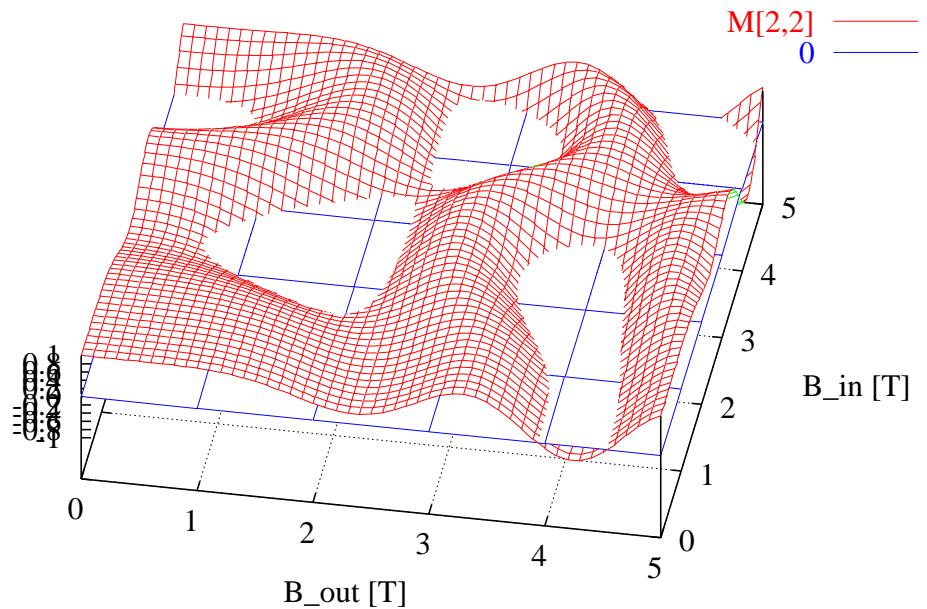
$$\Delta y = \begin{cases} 3.2 \text{ cm,} & \text{for protons} \\ -2.1 \text{ cm,} & \text{for He}^3 \end{cases}$$

Comparison of Rotators for He³ and p

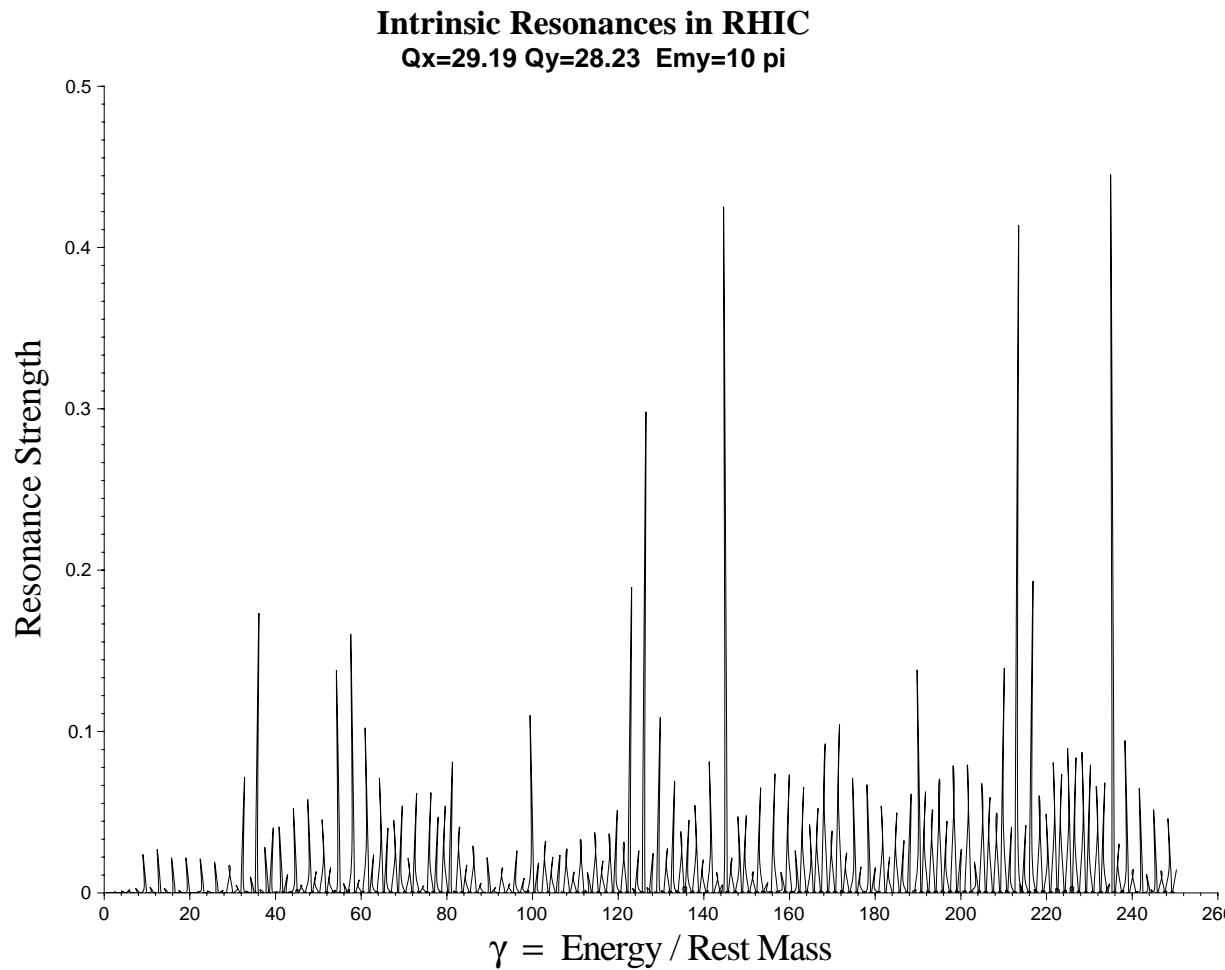
Spin rotator contours for protons at 250 GeV



Spin rotator contour for He3 at 500 GeV



Depolarizing Resonances for Protons



Will depolarize beam during acceleration.

Increase in strength with energy.

$$|G\gamma|_{\max} = \begin{cases} 477, & \text{p} \\ 743, & \text{He}^3 \end{cases}$$

↳ Summary ↳

- ~ Spin precession and orbit excursions in snakes and rotators should work for protons eRHIC.
 - Snakes the same for protons.
 - If no “D0DX” bends for IR, then fields in rotators are essentially constant for all energies (like the snakes).
- ~ He³ requires less field in snakes and rotators.
 - Injection orbit excursions reduced.
- ~ |G γ |_{max} is higher for He³.
 - This needs to be investigated.